Non-normal Amplification of the Thermohaline Circulation Laure Zanna^{*}, Eli Tziperman and Patrick Heimbach *Dept of Earth and Planetary Sciences, Harvard University, zanna@fas.harvard.edu **2 Model Description Mechanism:** Interaction of 5 eigenmodes with decaying time-scale from 20 to 800 years Fig.1: 2D zonally averaged Top View Side View (a) coupled ocn-atm model 90N Atmosphere (a) Top View: the -30 Land surfaceocean represents 70% Ocean Ocean of the total surface, (b) Side View: 2 vertical layers for the ocean; 90S West East 1 vertically integrated layer 90S 90N for the atmosphere. 0.2 (4) Atmosphere: Energy Balance Model (temperature & moisture) Ocean: Advection- Diffusion Equation for salinity and temperature. *Coupling*: Air-sea heat flux + freshwater flux The horizontal transport in the ocean (THC) is proportional to density gradients. (Stommel, 1961) Fig. 3: Principal eigenmodes participating in the transient amplification **3 Solving for optimal initial conditions** (e.g. Farrell, 1988) (a) Initial conditions for the 5 dominant eigenmodes contributing to the Linearization of the full nonlinear model about steady state transient growth of the THC anomalies. Eigenmodes with decay time Linearized model: $\frac{d\vec{P}}{dt} = A\vec{P}$, $\vec{P}'(t) = e^{At}\vec{P}_0$ where $\vec{P}' = [\boldsymbol{q}', \boldsymbol{q}', T', S']_{1\times 366}^T$ scale of (1) 23 years, (2) 25 years, (3) 87 years, (4) 281 years, (5) 784 years; (b) (6)-(10) Time evolution of the THC anomalies resulting from the initial anomalies (1)-(5). • Maximize THC anomaly $\int |THC'(t, y)|^2 dy$ over both hemispheres **5.2 Mechanism : amplification is due to the advection of** at t=t, to find optimal initial conditions \vec{P}_0 under a given norm. the mean flow by the THC anomalies is stable, it grows ! Solving the generalized eigenproblem for the optimal i.c P_0 . (a) THC anomaly [Sv] **Results: DRAMATIC AMPLIFICATION** of the THC, TEMPERATURE and SALINITY anomalies before eventually decaying. after 42 years. Fig. 2: Linearized model evolution (a) T_{top} anomaly [° C] starting from the optimal initial conditions resulting in a maximum amplification of the 60 before eventual decay Latitude [° THC after 42 years. The variables Fig. 4: Evolution of the THC anomalies in different experiments as a are shown as a fct of time and -0.04 function of latitude and time, (a) a model experiment where $v\nabla T'$ latitude. -0.06 and $v\nabla S'$ are eliminated, (b) a model experiment where $v'\nabla T$ (a) surface temperature (grows by a and $v'\nabla S$ are eliminated. Both T and S are critical to this factor of ~ 400), (b) surface salinity (grows by a factor mechanism, unlike in typical THC instability. of ~20), Latitude [°] **5** Conclusions (c) THC anomalies. (b) S_{top} anomaly [ppt] (c) THC anomaly [Sv] We found a mechanism for transient growth of the THC anomaly with a time scale of ~40yrs Time •THC (t=0)=0 (T' / S' mutually cancelled) •Dramatic growth of THC & model variables Time [yrs] •Interaction of fast & slow decaying eigenmodes •Growth due to advection of the mean flow by the THC perturbations •*Small* initial perturbations ? *Large* amplification !

60 90

Abstract

- possible transient amplification of the thermohaline circulation (THC).
- We find that in a stable regime, in which all small perturbations eventually decay, optimal initial conditions lead to a dramatic **amplification of the THC anomalies**, as well as of the temperature and salinity anomalies (amplified by factors of 400 and 20 respectively) after ~ 40 years. The anomalies eventually decay on a centennial time scale.
- Such large amplification of small initial anomalies of the THC, temperature and salinity may play an important role in the THC and climate variability if excited by atmospheric forcing.

Introduction

- The **THC** appears to have been fairly stable with a small amplitude variability for the past 10,000 years. Its variability might be described by linear dynamics excited by stochastic forcing (e.g. Griffies and *Tziperman, 1995).*
- Non normal growth and transient amplification Non-normal stable linear system = set of non-orthogonal decaying eigenvectors \Rightarrow may lead to transient amplification due to an interaction between several decaying eigenmodes of the system.
- 2D example:



Conditions for transient amplification in a stable linear system

- . Non-orthogonal eigenvectors
- 2. Partial initial cancellation
- 3. Different decay rates of

the eigenvectors

(e.g. Farrell & Ioannou, 1996, previous application to the THC in a simple box model by Tziperman & Ioannou, 2002 ; Lohmann & Schneider, 1999 or to ENSO by Moore & Kleeman, 1997 and Penland & Sardeshmukh, 1995)



References

Farrell, B.F. and P.J. Ioannou, 1996: Generalized stability theory part I: Autonomous operators. J. Atmos. Sci., 53, 2025-2040; Farrell, B. F., 1988: Optimal excitation of neutral Rossby waves. J. Atmos. Sci., 45, 163-172; Griffies, S. M. and E. Tziperman, 1995: A linear thermohaline oscillator driven by stochasting atmospheric forcing. J. Climate, 8, 2440-2453; Moore, A M. and R. Kleeman, 1997: The singular vectors of a coupled ocean-atmosphere model of ENSO. Q. J. R. Meteor. Soc., 123, 953-1006; Penland, C. and P.D. Sardeshmukh, 1995: The optimal-growth of tropical sea-surface temperature anomalies. J Climate, 8, 1999-2024; Stommel, 1961: Thermohaline convection with two stable regimes of flow. Tellus, 13, 224-230; Tziperman, E. and P. J. Ioannou, 2002: Transient growth and optimal excitation of thermohaline variability. J. Phys. Oceanog., 32, 3427-3435; Zanna and Tziperman, 2005: Non-normal amplification of the thermohaline circulation. J. Phys. Oceanog., 35, 1593-1605

variability if excited by atmospheric forcing.

